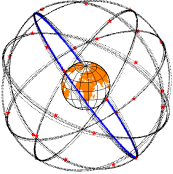


Reference Frame Realization Lecture 05

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Reference Frames



Global
Center of Mass ~ 30 mm
ITRF ~ 2 mm, < 1 mm/yr

Continental
< 1 mm/yr horiz., 2 mm/yr vert.

Local -- may be self-defined

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Reference frames in Geodetic Analyses

- Output from GAMIT
 - Loosely constrained solutions
 - Relative position well determined, "Absolute position" weakly defined
 - Need a procedure to expressed coordinates in a well defined reference frame
- Two aspects
 - Theoretical (e.g., rigid block, mantle-fixed, no-net-rotation of plates)
 - Realization through a set of coordinates and velocities
 - "finite constraints": a priori sigmas on site coordinates
 - "generalized constraints": minimize coordinate residuals while adjusting translation, rotation, and scale parameters
- Three considerations in data processing and analysis
 - Consistent with GPS orbits and EOP (NNR)
 - not an issue if network small or if orbits and EOP estimated
 - Physically meaningful frame in which to visualize site motions
 - Robust realization for velocities and/or time series

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Basics of reference frame realization

- In nearly all cases, it is best to leave sites loosely constrained in globk and then use glorg to realize the reference frame.
- Normally, realization is rotation and translation to align to specific set of coordinates and velocities.
- The glorg algorithm requires system be free to rotate and translate. In gamit "baseline" processing:

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GLOBK frame realization methods

- In GLOBK analyses, normally all stations and orbit initial conditions are loosely constrained, the reference frame is defined in a module called glorg (global origin). The methods used are similar to other programs but there are some subtle differences. Specifically, the frame transformation is implement with a Kalman filter constraint equation, not by direct application of the rotations, translations and scale.
- Details are discussed in Dong, Herring and King, J. Geodesy, 1998.

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Specific implementation

- Glorg computes a set of condition equations using weighted least squares. The weights are settable to be dependent on site uncertainty (iteratively) and with weight between horizontal and vertical site positions and rates.
- The condition equations are then applied through a Kalman filter formulation to the loose solution covariance matrix and solution vector. The KF formulation allows zero variance for the condition (LSQ approach would need a small but finite variance). The condition can also be given finite variance (avoids zero eigenvalues).
- If the original loose solution is free to translate, rotate and scale, the application of the condition solution generate the same answer explicit application of transformation (SDET option).
 - For VLBI, translation is rank deficient and rotation is explicitly estimated (scale needs to be explicitly estimated if included in the constraints)
 - For GPS, translation is not rank deficient and so condition modifies solution if translation not explicitly estimated. It is not clear whether translation should be estimated explicitly.

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Formulation

- Condition application, T are estimates of transformation parameters, W is weight matrix, and superscript – and + denote values before and after the conditions are applied. R is the variance of the condition and can be set to zero. (MIT weekly IGS sinex submission, sets 1 m² on translation so not forced to zero)

$$\begin{aligned} \bar{T} &= (A^T W A)^{-1} A^T W \Delta X_s = H \Delta X_s \\ \Delta X^+ &= P^- H^T [H P^- H^T + R]^{-1} (\Delta X^- - A \bar{T}) = K \delta X^- \\ P^+ &= [I - K H] P^- \end{aligned}$$

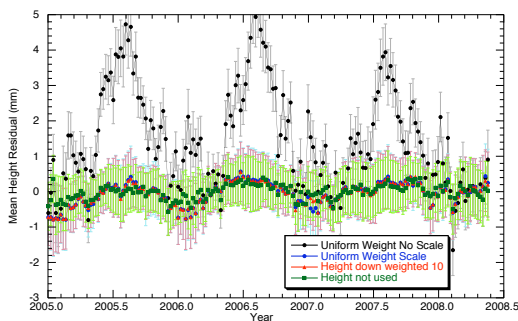
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Coordinate Weight effect

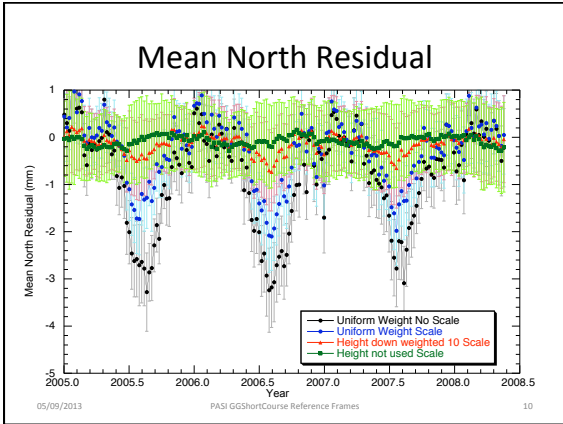
- Next set of slides show the effects of height weight on the means of site position residuals after transformation:
 - when uniform weight (i.e., height is weighted same as horizontal) is used with no scale estimated (mean height residual is scale)
 - when scale estimated with
 - Uniform height weight
 - Heights down weighted by 10 (consistent with sigmas, default)
 - Height so down weighted so much that effectively not used.

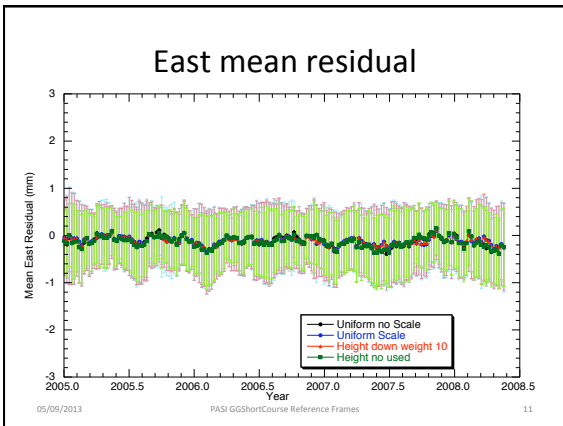
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Mean Heights



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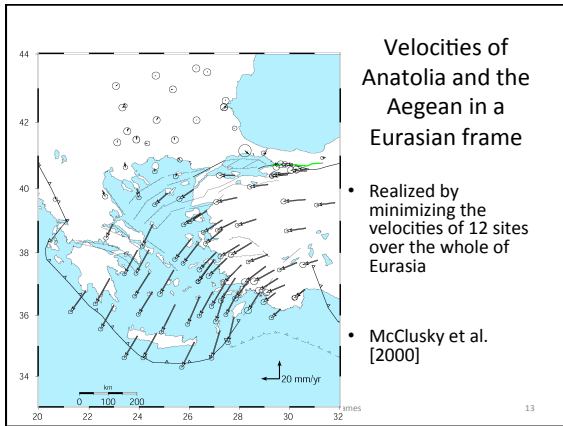


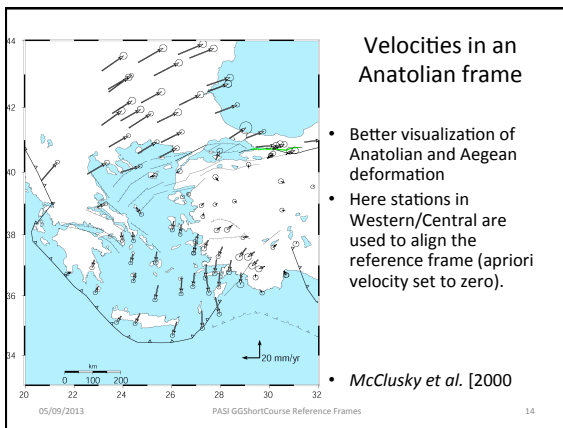


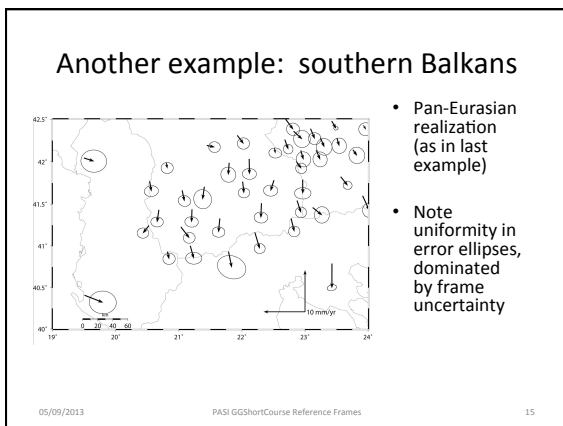
Local Frame Realization

- When dealing with a local region (100-3000 km in size), there are a number of choices of approach:
 - Sometime motion relative to a stable plate (e.g., Eurasia) is needed
 - Often since local strains are important, a local reference frame provides a more useful way of viewing results.
 - In the GLORG, translation/rotation method only the rotational part of the strain tensor is effected by how the reference frame is realized. (This is not the case when tight constraints are applied).

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Local Frame Realization

- Frame realization using 8 stations in central Macedonia
- Note smaller error ellipses within stabilization region and larger ellipses at edges

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Defining Reference Frames in GLOBK

- Three approaches to reference frame definition in GLOBK
 - Finite constraints (in globk, same as GAMIT)
 - Generalized constraints in 3-D (in glorg)
 - Generalized constraints for horizontal blocks (‘plate’ feature of glorg)
- Reference frame for time series
 - More sensitive than velocity solution to changes in sites
 - Initially use same reference sites as velocity solution
 - Final time series should use (almost) all sites for stabilization

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Frame definition with finite constraints

- Applied in globk (glorg not called): We do not recommend this approach since it is sensitive to over-constraints that can distort velocities and positions
- Example:


```
apr_file itr08.apr
apr_neu all 10 10 10 1 1 1
apr_neu algo .005 005 .010 .001 .001 .003
apr_neu pie1 .002 005 .010 .001 .001 .003
apr_neu drao .005 005 .010 .002 .002 .005
...
```
- Most useful when only one or two reference sites or very local area.
- Disadvantage for large networks is that bad a priori coordinates or bad data from a reference site can distort the network

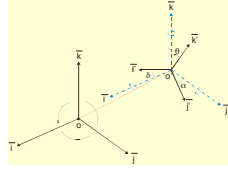
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Frame definition with generalized constraints

- Applied in *glorg*: minimize residuals of reference sites while estimating translation, rotation, and/or scale (3 -7 parameters)
- ```

apr_file itr05.apr
pos_org xtran ytran ztran xrot yrot
zrot
stab_site algo pie1 drao ...
cnd_hgtv 10 10 0.8 3.

```



- All reference coordinates free to adjust (anomalies more apparent); outliers are iteratively removed by *glorg*
- Network can translate and rotate but not distort
- Works best with strong redundancy (number and [if rotation] geometry of coordinates exceeds number of parameters estimated)
- Can downweight heights if suspect or to minimize loading effects

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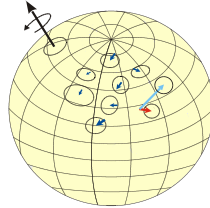
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### Referencing to a horizontal block ('plate')

- Applied in *glorg*: first stabilize in the usual way with respect to a reference set of coordinates and velocities (e.g. ITRF-NNR), then define one or more 'rigid' blocks
- ```

apr_file itr05.apr
pos_org xtran ytran ztran xrot yrot zrot
stab_site algo pie1 nlib drao gold sni1 mkea chat
cnd_hgtv 10 10 0.8 3.
plate_noam algo pie1 nlib
assign_p_noam drao fair
plate_pcfc sni1 mkea chat
    
```

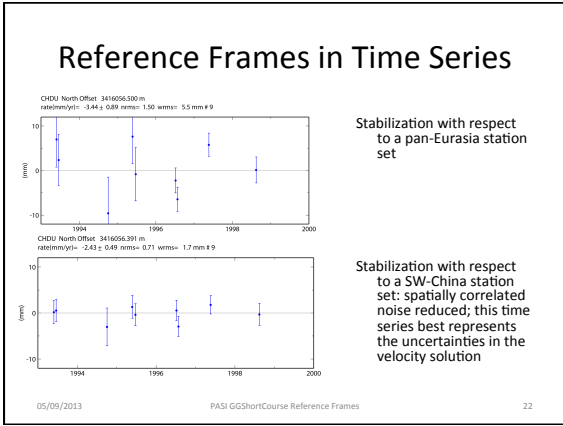


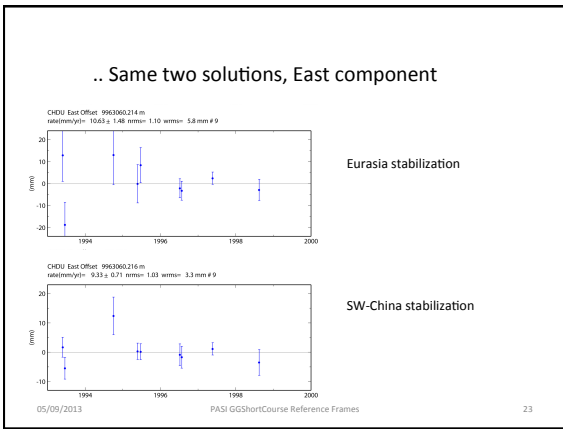
After stabilization, *glorg* will estimate a rotation vector ('Euler pole') for each plate with respect to the frame of the full stabilization set and print the relative poles between each set of plates

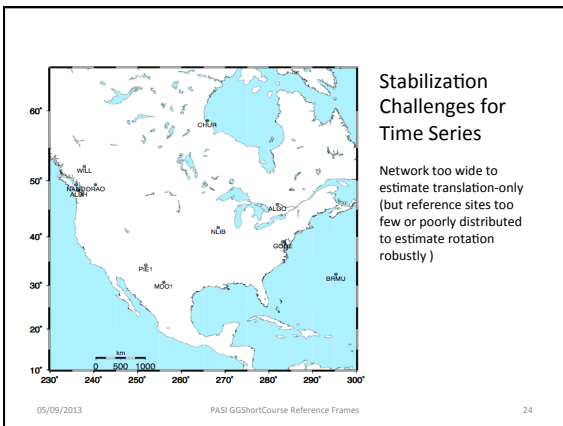
Use *sh_org2vel* to extract the velocities of all sites with respect to each plate

Rules for Stabilization of Time Series

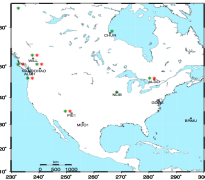
- Small-extent network: translation-only in *glorg*, must constrain EOP in *globk*
- Large-extent network: translation+rotation, must keep EOP loose in *globk*;
- if scale estimated in *glorg*, it must estimate scale in *globk*
- 1st pass for editing:
 - "Adequate" *stab_site* list of stations with accurate a priori coordinates and velocities and available most days
 - Keep in mind deficiencies in the list
- Final pass for presentation / assessment / statistics
 - Robust *stab_site* list of all/most stations in network, with coordinates and velocities determined from the final velocity solution
- System is often iterated (velocity field solution, generate time series, editing and statistics of time series; re-generate velocity field).



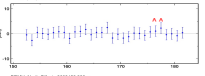




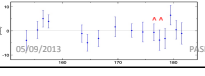
Stable reference frame



Example of time series for which the available reference sites changes day-to-day but is robust (6 or more sites, well distributed, with translation and rotation estimated)



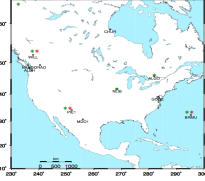
Day 176 ALGO PIE1 DRAO WILL ALBH
NANO
rms 1.5 mm



Day 177 ALGO NLIB CHUR PIE1 YELL DRAO
WILL ALBH NANO
rms 2.3 mm

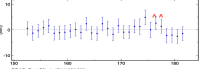
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Unstable case

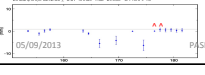


Example of time series for which the available reference sites changes day-to-day and is not robust (only 3 sites on one day)

NOTE: Distant frame definition sites can have very small error bars when used and large error bars when not used.



Day 176 BRMU PIE1 WILL
rms 0.4 mm



Day 177 BRMU ALGO NLIB PIE1
YELL WILL
rms 2.0 mm

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Use of Global binary H-files

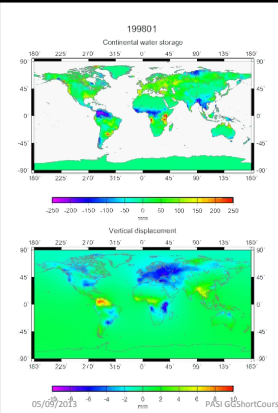
- Include global h-files ... or not? For post-2000 data not needed for orbits
- Advantages
 - Access to a large number of sites for frame definition
 - Can (should) allow adjustment to orbits and EOP
 - Eases computational burden
- Disadvantages
 - Must use (mostly) the same models as the global processing
 - Orbits implied by the global data worse than IGSF
 - Some bad data may be included in global h-files (can remove)
 - Greater data storage burden

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Regional versus Global stabilization

- If not using external h-files, use 8 or more well distributed sites reference sites
- If combining with MIT or SOPAC* global h-files, use 4-6 well-performing common sites (not necessarily with well-known coordinates),
- MIT hfiles available at ftp://everest.mit.edu/pub/MIT_GLL/HYY
When using MIT files, add apr_svant all F F F to globk command file to fix the satellite antenna offsets
- If SOPAC, use all 'igs' h-files to get orbits well-determined

Seasonal Effects



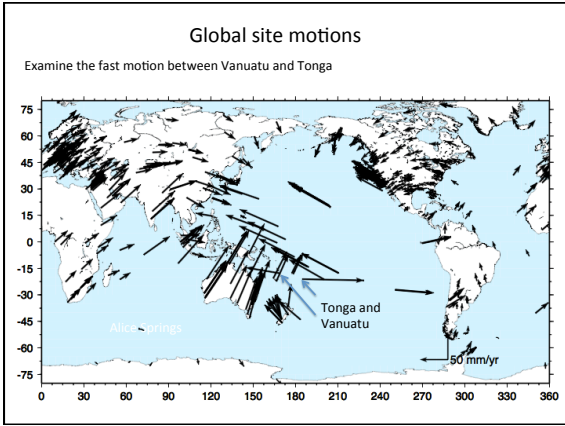
Large seasonal signals due to hydrological loading in many regions of the world

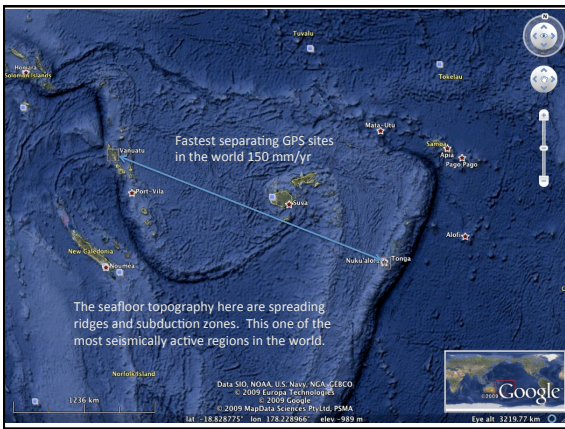
May generates spurious signals in time series

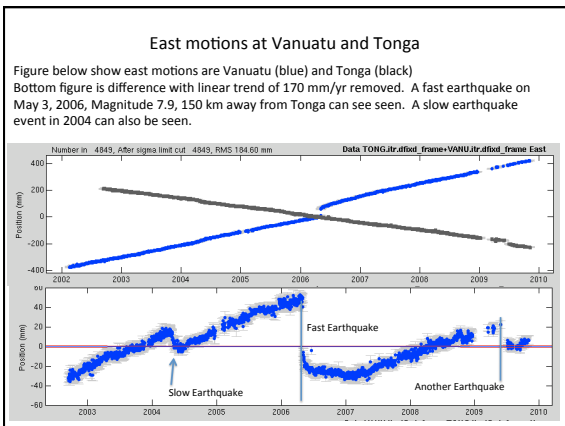
Courtesy J. P. Boy

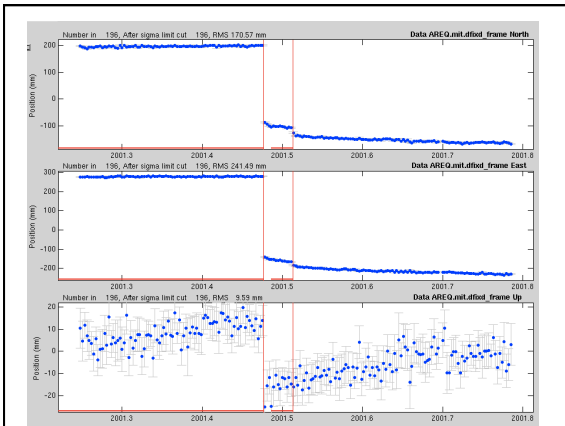
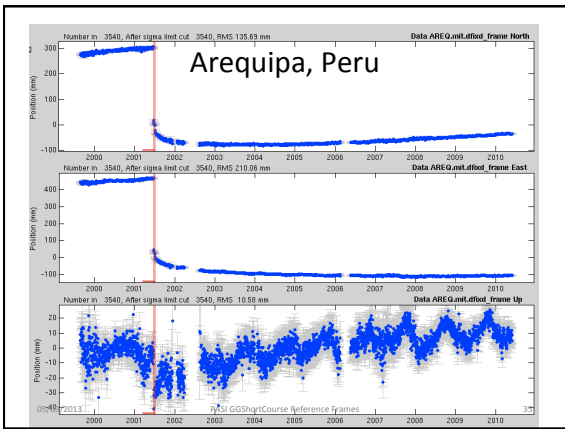
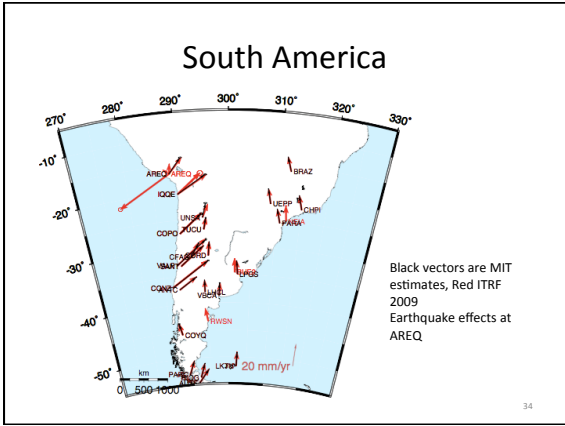
GRACE Results

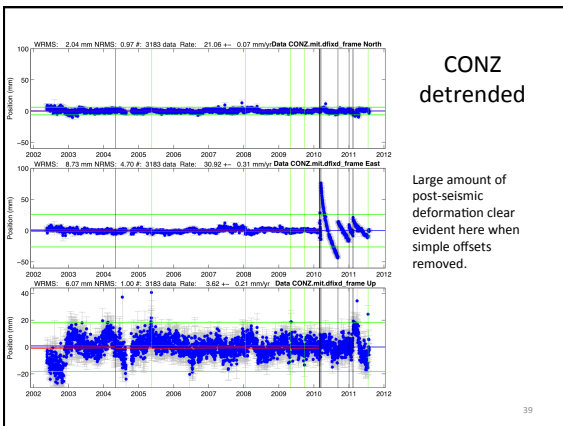
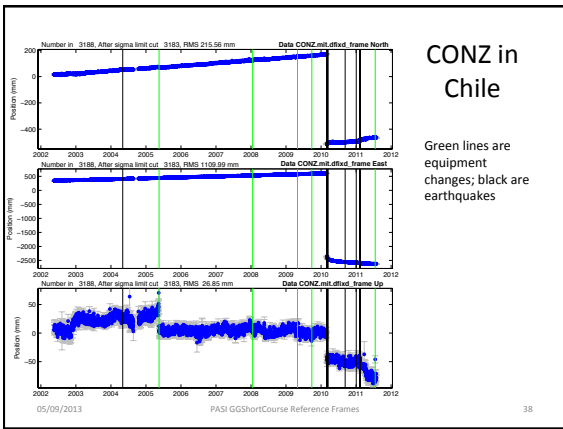
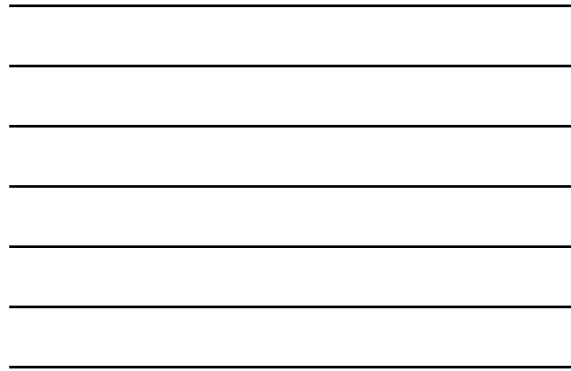
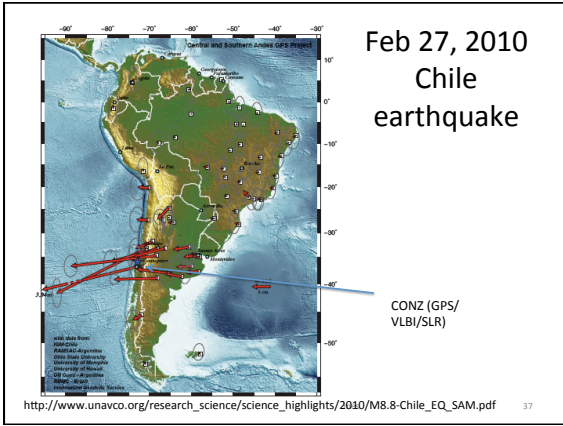
- There are number of web sites where GRACE results are available. For large-scale loading an approximate rule is 0.5 mm of vertical per mbar or cm of water
- Interactive site with graphics <http://geoid.colorado.edu/grace/grace.php>
- Also see site (select region and click on map): <http://grace.sgt-inc.com/>

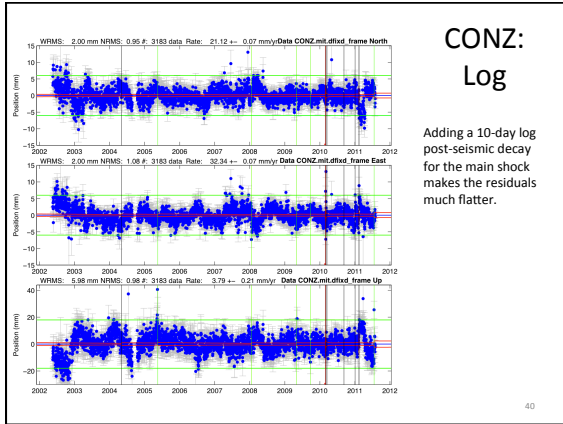






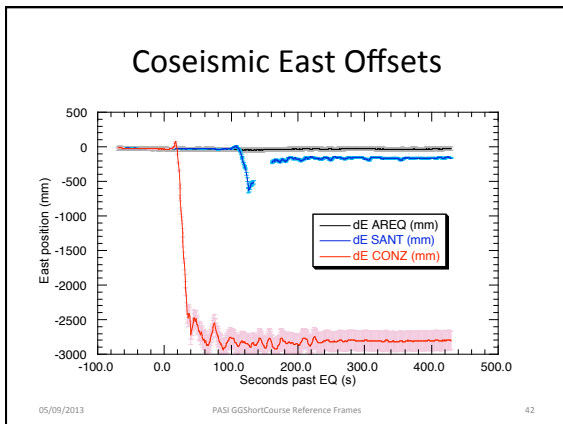
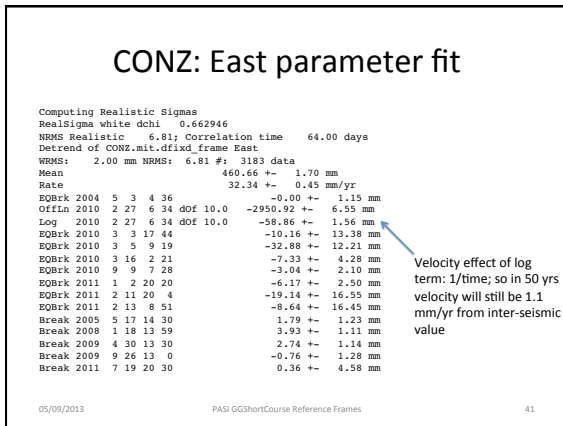
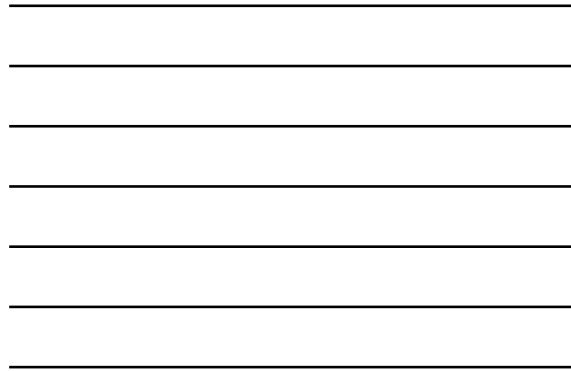






**CONZ:
Log**

Adding a 10-day log post-seismic decay for the main shock makes the residuals much flatter.



Summary

- Reference frame realization needs to be treated carefully in order to extract the most information from your GPS data analysis.
- The caution here is to carefully select and to process data from well distributed “stable” sites that can be used for the reference definition:
 - When we say a site or group of sites is moving, the reference frame defines what we consider to be the non-moving system to which the movement is referenced.

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